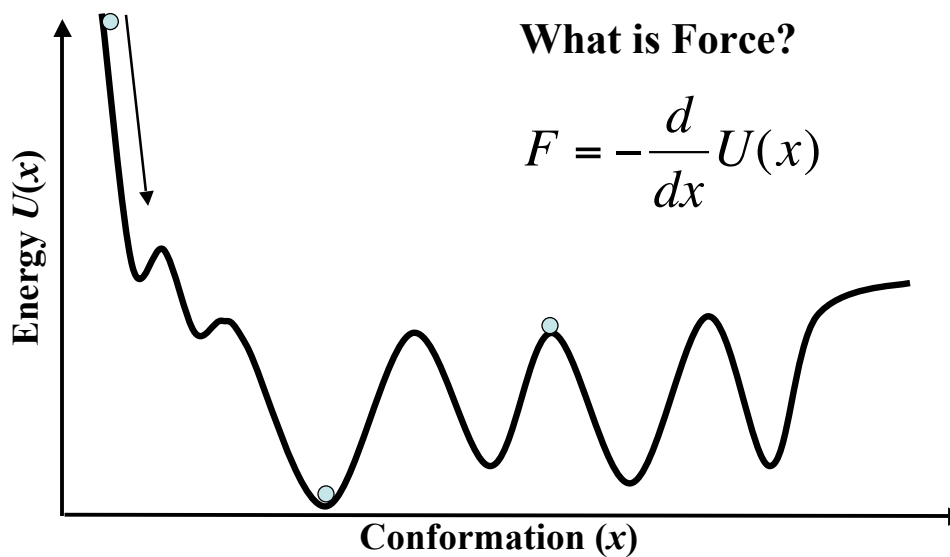


Don't forget to bring your MD tutorial

Lab session starts at 1pm

You will have to finish an MD/SMD exercise on α -conotoxin in oxidized and reduced forms

Potential Energy (hyper)Surface



Classical Molecular Dynamics

$$\mathbf{r}(t + \delta t) = \mathbf{r}(t) + \mathbf{v}(t)\delta t$$

$$\mathbf{v}(t + \delta t) = \mathbf{v}(t) + \mathbf{a}(t)\delta t$$

$$\mathbf{a}(t) = \mathbf{F}(t) / m$$

$$\mathbf{F} = -\frac{d}{dr}U(\mathbf{r})$$

CHARMM Potential Function

$$\begin{aligned}
 U(\vec{R}) = & \underbrace{\sum_{bonds} k_i^{bond} (r_i - r_0)^2}_{U_{bond}} + \underbrace{\sum_{angles} k_i^{angle} (\theta_i - \theta_0)^2}_{U_{angle}} + \\
 & \underbrace{\sum_{dihedrals} k_i^{dihe} [1 + \cos(n_i \phi_i + \delta_i)]}_{U_{dihedral}} + \underbrace{\sum_i \sum_{j \neq i} 4\epsilon_{ij} \left[\left(\frac{\sigma_{ij}}{r_{ij}} \right)^{12} - \left(\frac{\sigma_{ij}}{r_{ij}} \right)^6 \right]}_{U_{nonbond}} + \sum_i \sum_{j \neq i} \frac{q_i q_j}{\epsilon r_{ij}}
 \end{aligned}$$

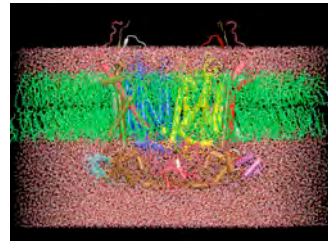
PDB file → geometry
 Topology PSF file
 parameters ← Parameter file

Preparing Your System for MD Solvation

Biological activity is the result of interactions between molecules and occurs at the interfaces between molecules (protein-protein, protein-DNA, protein-solvent, DNA-solvent, etc).

Why model solvation?

- many biological processes occur in aqueous solution
- solvation effects play a crucial role in determining molecular conformation, electronic properties, binding energies, etc



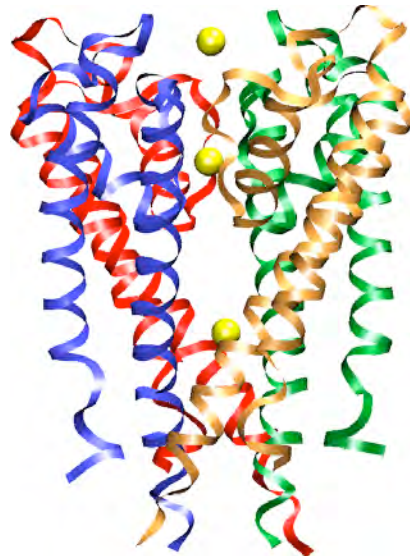
How to model solvation?

- explicit treatment: solvent molecules are added to the molecular system
- implicit treatment: solvent is modeled as a continuum dielectric

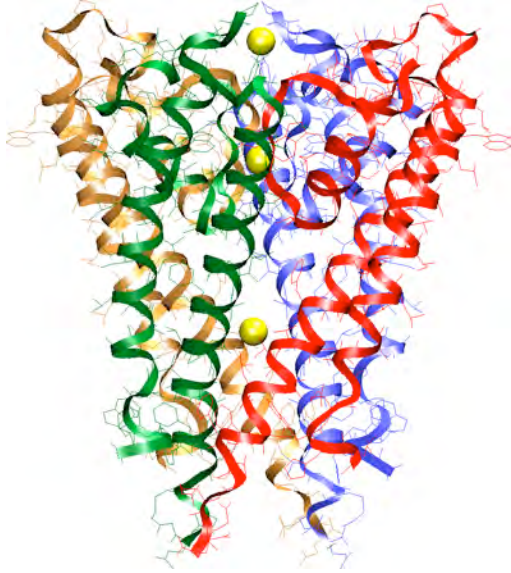
Example: MD Simulations of the K⁺ Channel Protein

Ion channels are membrane - spanning proteins that form a pathway for the flux of inorganic ions across cell membranes.

Potassium channels are a particularly interesting class of ion channels, managing to distinguish with impressive fidelity between K⁺ and Na⁺ ions while maintaining a very high throughput of K⁺ ions when gated.

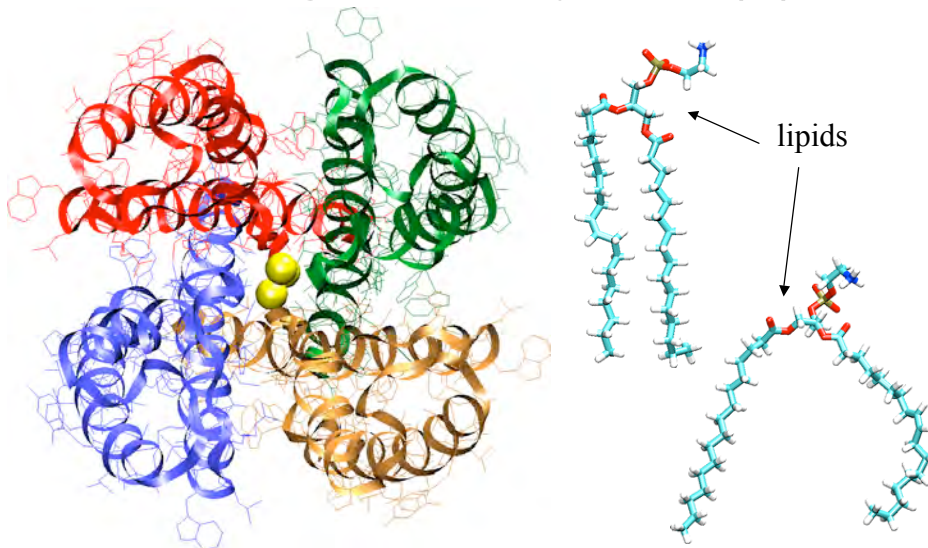


Setting up the system (1)



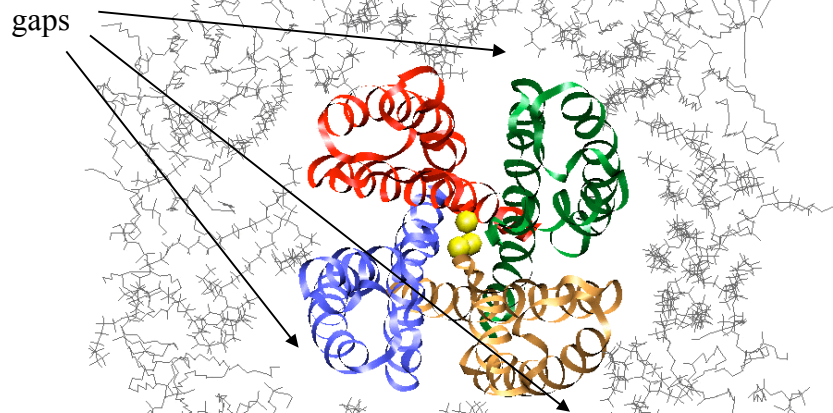
- retrieve the PDB (coordinates) file from the Protein Data Bank
- add hydrogen atoms using PSFGEN
- use topology and parameter files to set up the structure
- minimize the protein structure using NAMD2

Setting up the system (2)



Simulate the protein in its natural environment: solvated lipid bilayer

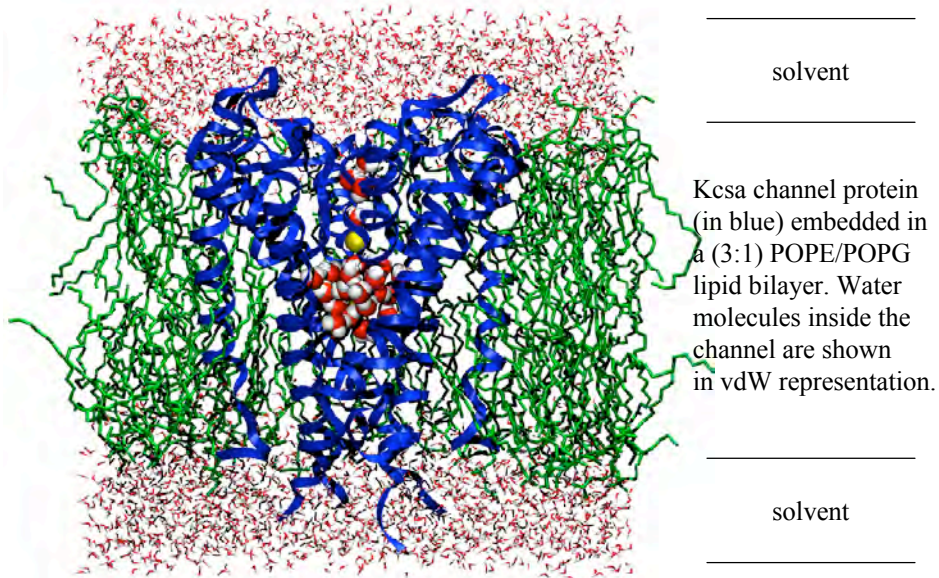
Setting up the system (3) Inserting the protein in the lipid bilayer

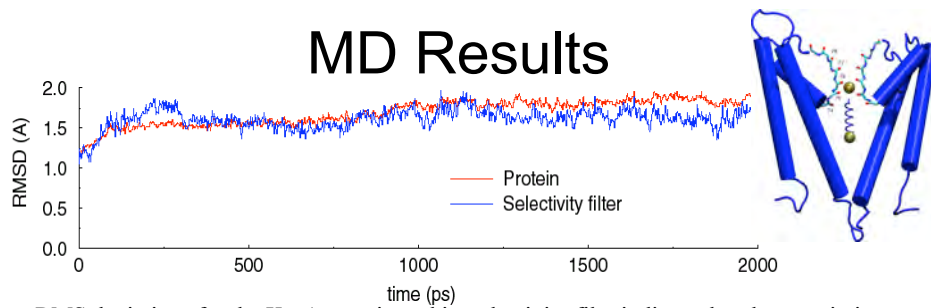


Automatic insertion into the lipid bilayer leads to big gaps between the protein and the membrane => long equilibration time required to fill the gaps.

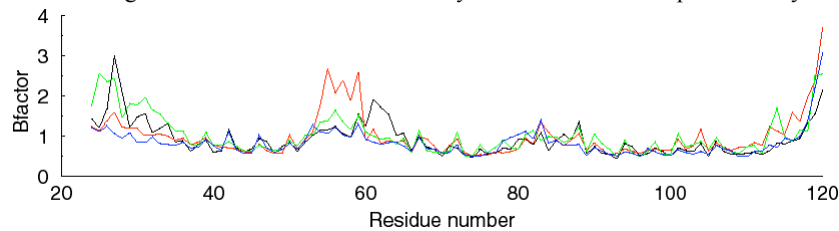
Solution: manually adjust the position of lipids around the protein

The system





RMS deviations for the KcsA protein and its selectivity filter indicate that the protein is stable during the simulation with the selectivity filter the most stable part of the system.



Temperature factors for individual residues in the four monomers of the KcsA channel protein indicate that the most flexible parts of the protein are the N and C terminal ends, residues 52-60 and residues 84-90. Residues 74-80 in the selectivity filter have low temperature factors and are very stable during the simulation.

Simulating the system: Free MD

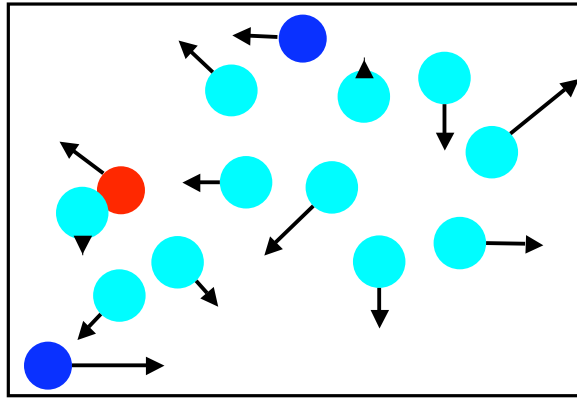
Summary of simulations:

- protein/membrane system contains 38,112 atoms, including 5117 water molecules, 100 POPE and 34 POPG lipids, plus K^+ counterions
- CHARMM26 forcefield
- periodic boundary conditions, PME electrostatics
- 1 ns equilibration at 310K, NpT
- 2 ns dynamics, NpT

Program: NAMD2

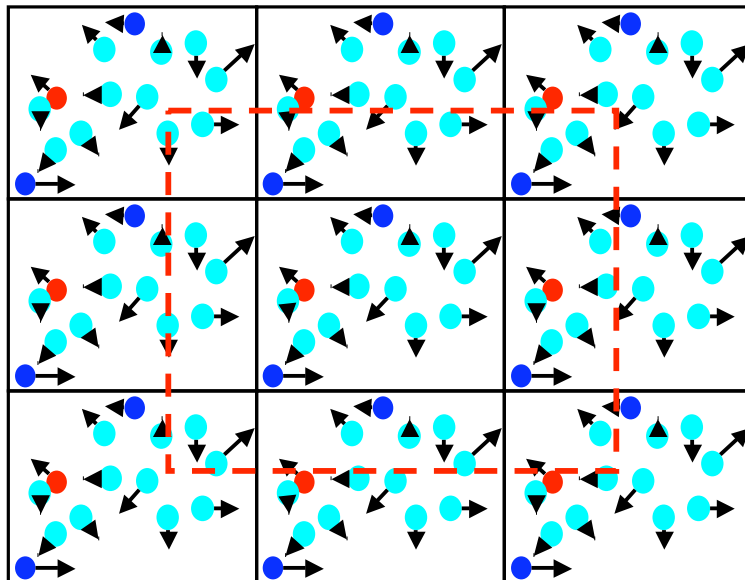
Platform: Cray T3E (Pittsburgh Supercomputer Center)

Boundary Conditions?



What happens if you put water under vacuum!?
Problems: Density, pressure, boundary effects, ...
One solution: reflective boundaries, not quite good.

Periodic Boundary Conditions

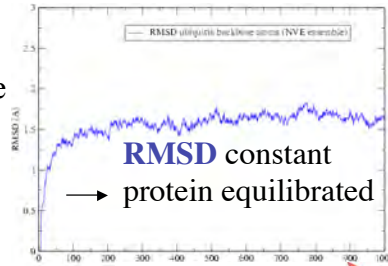


Equilibrium Properties of Proteins

Ubiquitin

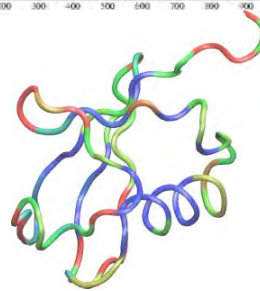
Root Mean Squared Deviation: measure for equilibration and protein flexibility

$$RMSD_{\alpha} = \sqrt{\frac{\sum_{j=1}^{N_t} \sum_{\alpha=1}^{N_{\alpha}} (\vec{r}_{\alpha}(t_j) - \langle \vec{r}_{\alpha} \rangle)^2}{N_{\alpha}}}$$



NMR structures
aligned together to see flexibility

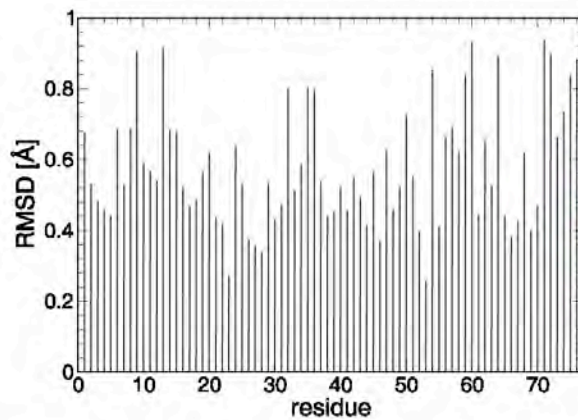
Protein sequence exhibits characteristic permanent flexibility!



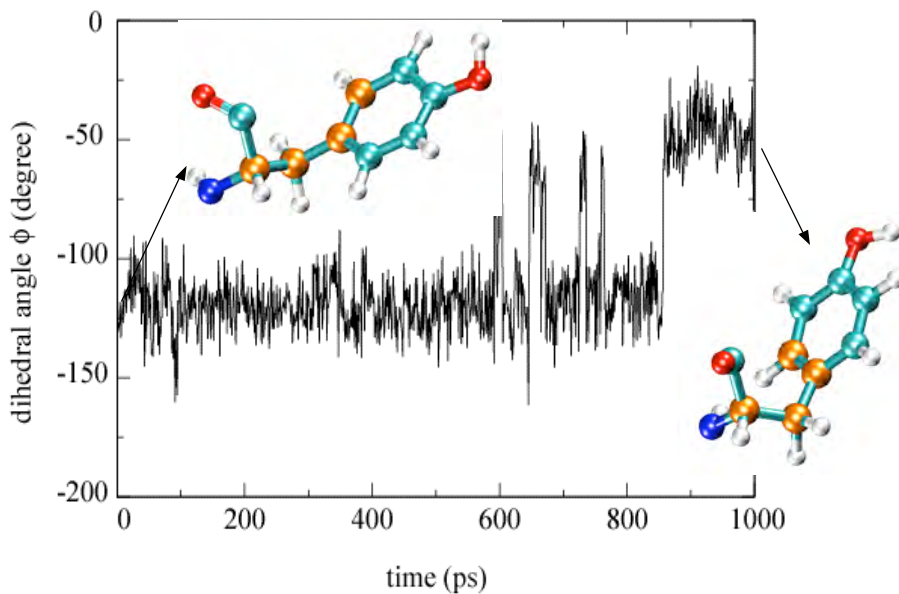
MD simulation
The color represents mobility of the protein through simulation (red = more flexible)

Thermal Motion of Ubiquitin from MD

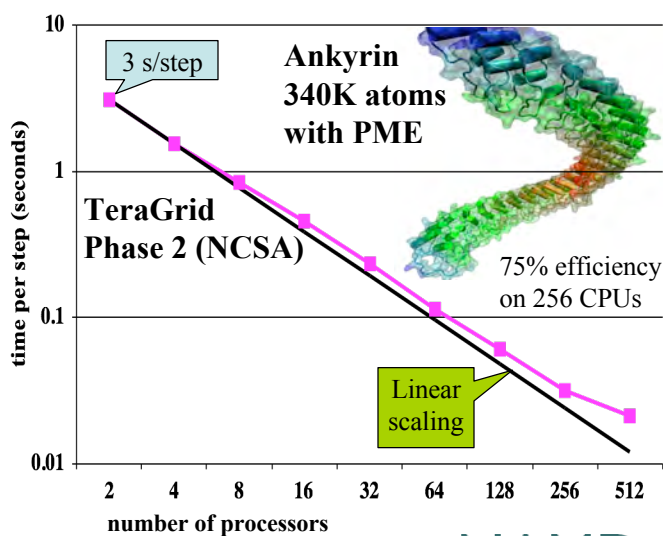
RMSD values per residue



Patience is required to observe Molecular Events



NAMD: The Program we will Use



J. Phillips Ph.D.

Simulation of large biomolecular systems

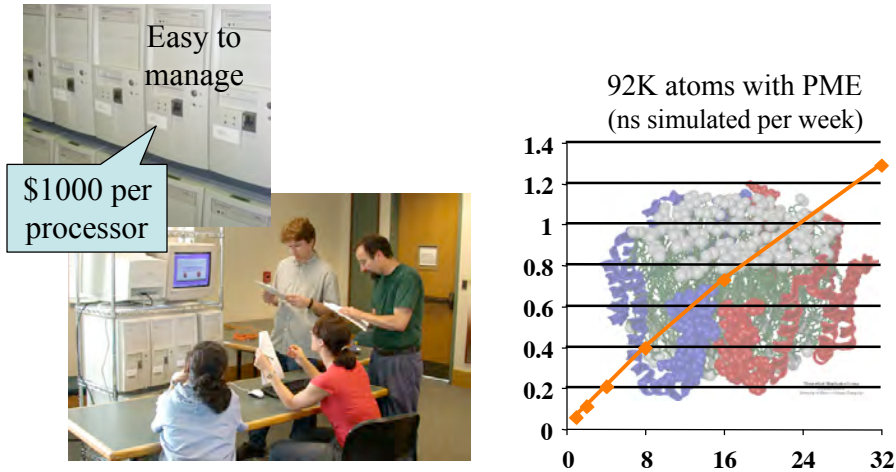
Runs at NSF centers, on clusters, and on desktop.

Available for **FREE** as precompiled binaries; includes source code.

NAMD
Scalable Molecular Dynamics

Linux Clusters

parallel computing on a professor's salary



The NAMD Configuration File / 1

Files needed:

```
structure      mypsf.psf
coordinates    mypdb.pdb
```

Define temperature

```
set temperature 310
    ;# target temperature used several times below
```

Starting simulation with random velocities

```
# starting from scratch
temperature      $temperature
    ;# initialize velocities randomly
```

The NAMD Configuration File / 2

Continuing a simulation with positions and velocities from previous run

```
# continuing a run
set inputname      myinput          ;# only need to edit this in one place!
binCoordinates     $inputname.coor  ;# coordinates from last run (binary)
binVelocities      $inputname.vel   ;# velocities from last run (binary)
extendedSystem     $inputname.xsc   ;# cell dimensions from last run
firsttimestep      50000            ;# last step of previous run
numsteps           100000           ;# run stops when this step is reached
```

The NAMD Configuration File / 3

Organizing output

```
outputName         myoutput
                  ;# base name for output from this run

restartfreq        500              ;# 500 steps = every 1ps
dcdfreq            500
xstFreq            500

outputEnergies     100              ;# 100 steps = every 0.2 ps
outputTiming       1000
                  ;# shows time per step and time to completion
```

The NAMD Configuration File / 4

```
# Force-Field Parameters
paraTypeCharmm    on
parameters        par_all27_prot_lipid.inp

# These are specified by CHARMM
exclude           scaled1-4
1-4scaling        1.0
switching         on

# You have some freedom choosing the cutoff
cutoff            12. ;# may use smaller, maybe 10., with PME
switchdist        10. ;# cutoff - 2.

# Promise that atom won't move more than 2A in a cycle
pairlistdist      14. ;# cutoff + 2.
stepspcycle       10  ;# redo pairlists every ten steps

# Integrator Parameters
timestep          2.0 ;# 2fs/step
rigidBonds        all ;# needed for 2fs steps
nonbondedFreq     1   ;# nonbonded forces every step
fullElectFrequency 2   ;# PME only every other step
```

12A cutoff is official standard for CHARMM force field but smaller is OK when using full electrostatics


Energy drifts if too large, but smaller requires more steps per ns.

The NAMD Configuration File / 5

Controlling temperature

```
{\small \begin{verbatim}
# Constant Temperature Control
langevin          on                ;# langevin dynamics

langevinDamping   5.                ;# damping coefficient of 5/ps
langevinTemp      $temperature      ;# random noise at this level
langevinHydrogen  no                ;# don't couple bath to hydrogens
```



Underlying Langevin equation for all atoms

$$m_i \frac{d^2 x_i(t)}{dt^2} = F_{i,\text{ff}} - \gamma m_i \frac{dx_i(t)}{dt} + R_i(t)$$

$$\langle R_i(t) R_i(t') \rangle = 2k_B T_{\text{target}} \gamma_i \delta(t - t')$$

The NAMD Configuration File / 6

Using periodic boundary conditions
(avoids surface effects; permits Particle-Mesh-Ewald (PME) electrostatics; permits pressure control)

```
# Periodic Boundary conditions
cellBasisVector1 31.2 0. 0. ;# vector to the next image
cellBasisVector2 0. 44.8 0.
cellBasisVector3 0. 0 51.3
cellOrigin 0. 0. 0. ;# the *center* of the cell

wrapWater on ;# wrap water to central cell
wrapAll on ;# wrap other molecules too
wrapNearest off ;# use for non-rectangular cells
```

The NAMD Configuration File / 7

Particle-Mesh-Ewald electrostatics
(avoids cut-off of long-range Coulomb forces)

```
#PME (for full-system periodic electrostatics)
PME yes
PMEGridSizeX 32 ;# 2^5, close to 31.2
PMEGridSizeY 45 ;# 3^2 * 5, close to 44.8
PMEGridSizeZ 54 ;# 2 * 3^3, close to 51.3
```

The NAMD Configuration File / 9

Fix atoms

```
fixedAtoms      on
fixedAtomsFile  myfixedatoms.pdb  ;# flags are in this file
fixedAtomsCol   B                  ;# set beta non-zero to fix an atom
```

The NAMD Configuration File / 10

Energy-minimize structure (T=0) , reset temperature T, run:

```
minimize      1000      ;# lower potential energy for 1000 steps
reinitvels    $temperature ;# since minimization zeros velocities
run 50000 ;# 100ps
```

The NAMD Output File / 1

Preamble

```
Info: NAMD 2.5b2ss03 for Linux-i686-Clustermatic
Info:
Info: Please visit http://www.ks.uiuc.edu/Research/namd/
Info: and send feedback or bug reports to namd@ks.uiuc.edu
Info:
Info: Please cite Kale et al., J. Comp. Phys. 151:283-312 (1999)
Info: in all publications reporting results obtained with NAMD.
Info:
Info: Built Fri May 30 13:09:06 CDT 2003 by jim on umbriel
Info: Sending usage information to NAMD developers via UDP.
Info: Sent data is: 1 NAMD 2.5b2ss03 Linux-i686-Clustermatic 47 umbriel jim
Info: Running on 47 processors.
```

The NAMD Output File / 2

Energies

ETITLE:	TS	BOND	ANGLE	DIHED	IMPRP
	ELECT	VDW	BOUNDARY	MISC	KINETIC
	TOTAL	TEMP	TOTAL2	TOTAL3	TEMPAVG
	PRESSURE	GPRESSURE	VOLUME	PRESSAVG	GPRESSAVG
ENERGY:	1000	0.0000	0.0000	0.0000	0.0000
	-97022.1848	9595.3175	0.0000	0.0000	14319.5268
	-73107.3405	300.2464	-73076.6148	-73084.1411	297.7598
	-626.5205	-636.6638	240716.1374	-616.5673	-616.6619

The NAMD Output File / 1

Writing out trajectories

```
⋮  
OPENING COORDINATE DCD FILE  
WRITING COORDINATES TO DCD FILE AT STEP 1000  
⋮
```

Performance information

Info: Benchmark time: 47 CPUs 0.0475851 s/step 0.275377 days/ns 13540 kB memory

TIMING: 1000 CPU: 18.35, 0.01831/step Wall: 50.1581, 0.0499508/step, 6.92374 hours remaining, 14244 kB of memory in use.

Warnings

Warning: Pairlistdist is too small for 1 patches during timestep 17.

Warning: Pairlists partially disabled; reduced performance likely.

Warning: 20 pairlist warnings since previous energy output.

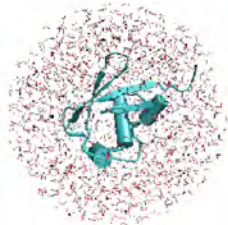
NAMD Example 1

You will first simulate ubiquitin in a water sphere and water box:

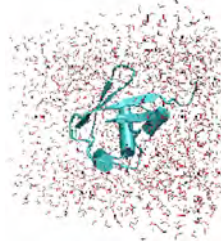
Generating a Protein Structure File (PSF)

- Go to 1-1-build directory
- Open VMD, choose extension TkCon
- Make from 1UBQ.pdb a structure without hydrogens, ubqp.pdb
- Create psf file for ubqp.pdb: ubq.pdb and ubq.psf
- Check if files exist

Solvate the protein in a water sphere (from VMD)



Solvate the protein in a water box (from VMD)



NAMD

- **RMSD value for equilibration**
- **Atomic RMSD values of equilibrated protein**
- **Velocity distribution**
- **Temperature distribution**

Inspection of the Results in VMD

- What to load?
 - Some basic analysis tools
 - Distances, angles,
 - Salt bridges
 - Fluctuations (RMSD) various types
 - Using Tcl scripting to repeat the analysis for all frames loaded.
-
- Example of BPTI

Inspection of the Results in VMD

- Animating the results
- Smoothing the trajectory
- Making figures and movies
- Simultaneous display of multiple frames

Major Difficulties in Simulating Biological Systems

"Size" problem

Biological Systems are Complex

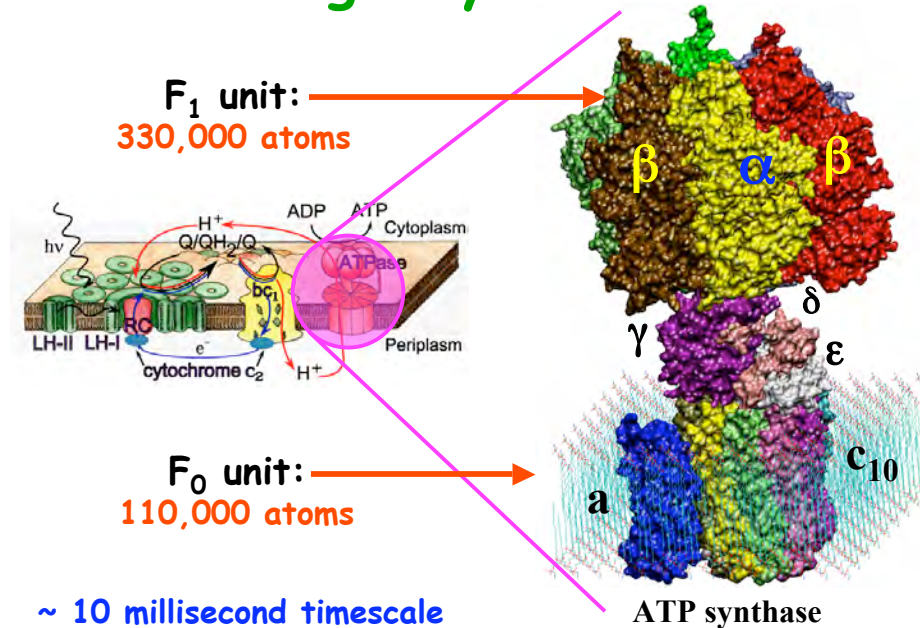
- Natural environment:
Membrane, solvent, ions, ...
- Many biosystems function in assemblies
Photosynthetic apparatus
Nuclear receptors, GPCRs, ...

"Time scale" problem

Many biological events happen at μs - ms time scales

- Signaling and other regulatory mechanisms
- Protein folding

Large Systems



Size scale can be addressed effectively by larger clusters of computers

HP 735 cluster
12 processors
(1993)



SGI Origin 2000
128 processors (1997)



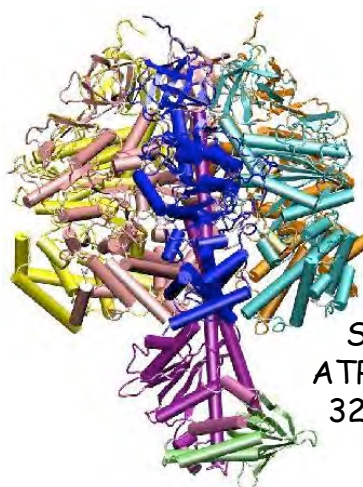
PSC LeMieux AlphaServer SC
3000 processors (2002)

Moving to Larger Molecules and Cellular Machines

BPTI
3K atoms
(1993)



Estrogen Receptor
36K atoms (1996)



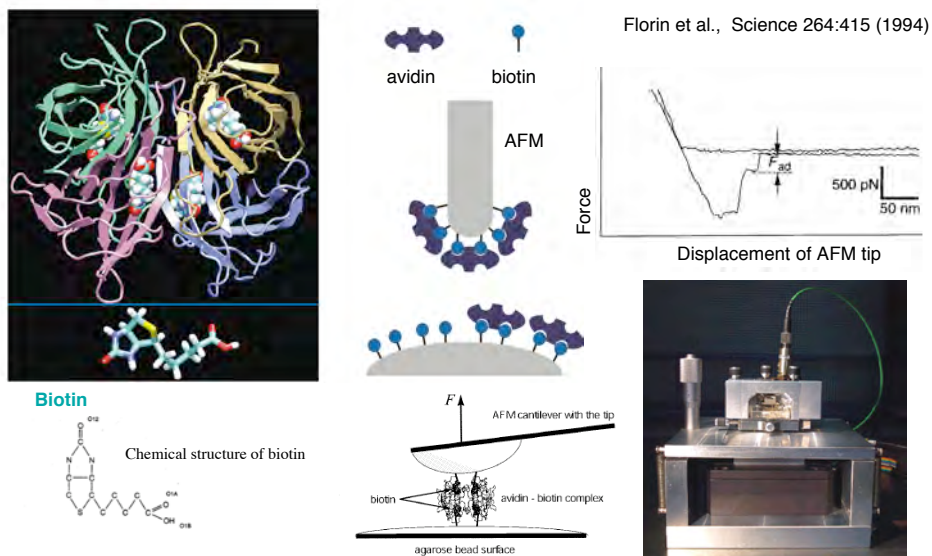
Solvated
ATP Synthase
327K atoms
(2002)

Time scales of several ns (100k) to μ s (10k), but ...

Steered Molecular Dynamics

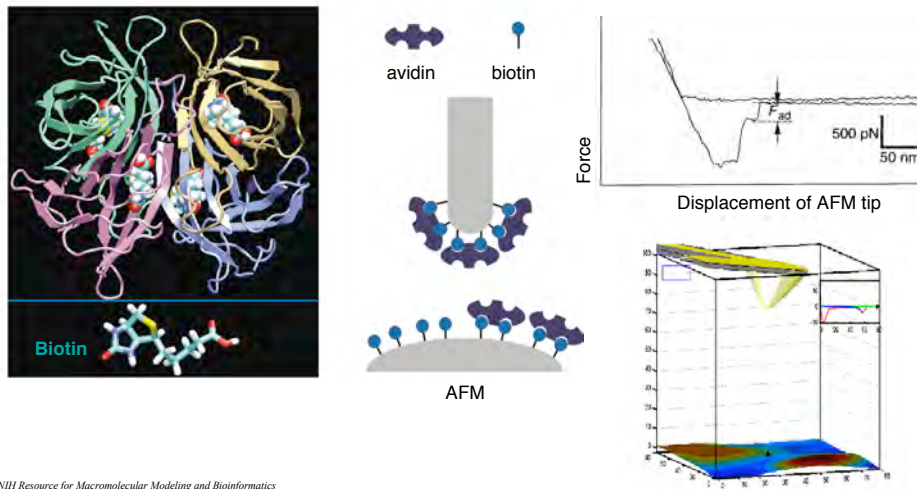
- Single Molecule Experiments: AFM
- Accelerating Events
 - Ligand Binding/Unbinding
 - Unfolding Experiments
 - Applying Surface Tension
 - **Torque Application**
 - Pressure induction
 - Inducing Large Domain Conformational Changes
- Constant-force: $f(t) = C$
- Constant-velocity: $f(t) = k [vt - (x_t - x_0)]$

Atomic Force Microscopy Experiments of Ligand Unbinding



Atomic Force Microscopy Experiments of Ligand Unbinding

Florin et al., Science 264:415 (1994)



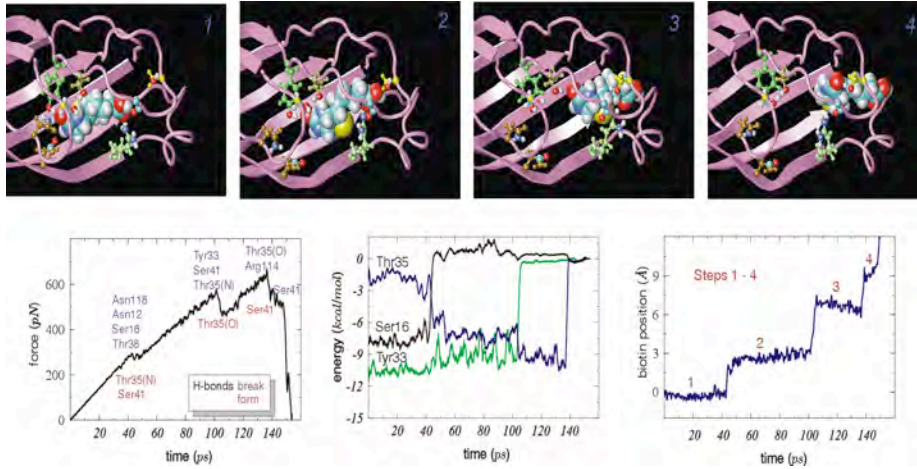
Pulling Biotin out of Avidin



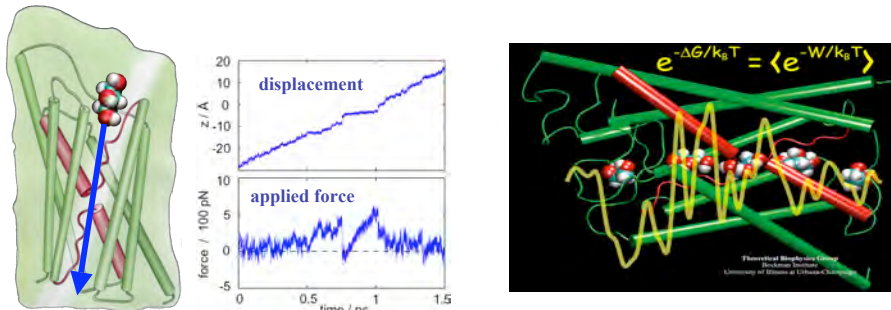
Molecular dynamics study of unbinding of the avidin-biotin complex. Sergei Izrailev, Sergey Stepaniants, Manel Balsera, Yoshi Oono, and Klaus Schulten. *Biophysical Journal*, 72:1568-1581, 1997.

SMD of Biotin Unbinding: What Was Learnt

biotin slips out in steps, guided by amino acid side groups, water molecules act as lubricant, MD overestimates extrusion force



Quantitative Analysis of Substrate Permeation



Jensen et al, *PNAS* 99: 6731-6736 (2002)

Calculation of the free energy profile of sugar transport from SMD simulations by Jarzynski's identity

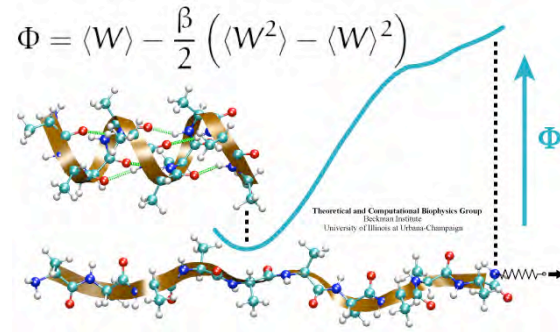
Thermodynamics: $\Delta G \leq \langle W \rangle$

Is there any chance to discount the irreversible work? Yes!

Free Energy of Stretched Alpha-Helix

Thermodynamics: $\Delta G \leq \langle W \rangle$

Jarzynski (1997): $e^{-\Delta G/k_B T} = \langle e^{-W/k_B T} \rangle$



Free energy calculation from steered molecular dynamics simulations using Jarzynski's equality. S. Park, F. Khalili-Araghi, E. Tajkhorshid, and K. Schulten. *Journal of Chemical Physics*, 119:3559-3566, 2003

Calculating potentials of mean force from steered molecular dynamics simulations. S. Park and K. Schulten. *Journal of Chemical Physics*, 120: 5946-5961, 2004